

# Electrodynamics of granular aluminum from superconductor to insulator: observation of collective superconducting modes

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work done with



A. Monfardini's group



MagSup team members



A. Gomez



I. Pop's group



B. Sacépé's group

# Outline

- Introduction :  
collective superconducting modes
- NEW* • Optical spectroscopy with superconducting resonator
- Study of granular aluminum versus  $\rho$ :
  - phase diagram SIT:  $\Delta$ ,  $T_c$ ,  $J$ ,  $E_c$
  - various sub-gap optical absorptions for  $h\nu < 2\Delta$

# Superconducting collective modes

Superconductivity: condensate of electrons with a *unique* phase

$$|\Psi|e^{i\theta}$$

breaking the rotational U(1) symmetry.

|                       |  |
|-----------------------|--|
| $ \Psi $ -fluctuation | $\theta$ -fluctuation                          |
| “Higgs” mode          | “Goldstone” mode                               |
| $E=2\Delta$           | $E=0$ or $\omega_{\text{plasma}}^* \gg \Delta$ |

at  $q=0$

Both modes optically inactive  
in conventional superconductor

BUT...

\*with Coulomb interaction

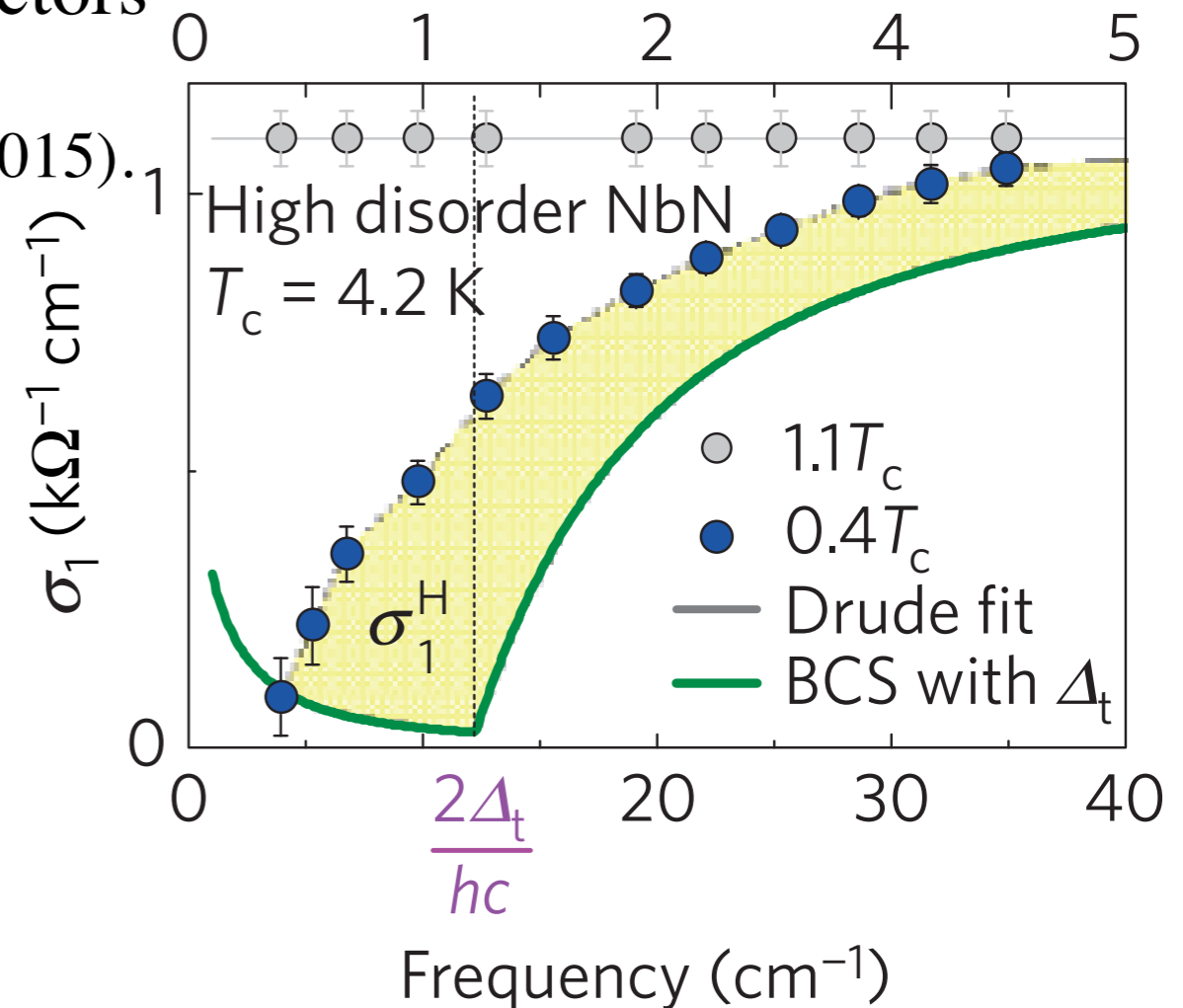
# Below $2\Delta$ : Higgs or Goldstone mode?

Excess of optical absorption below  $2\Delta$  interpreted as:

nature  
physics

The Higgs mode in disordered superconductors  
close to a quantum phase transition

D. Sherman and al, Nature Physics 11, 188–192 (2015).



PRB

Optical signatures of the superconducting Goldstone mode  
in granular aluminum: experiments and theory

U. S. Pracht and al, Phys. Rev. B 96, 094514 (2017).

# Below $2\Delta$ : Higgs or Goldstone mode?

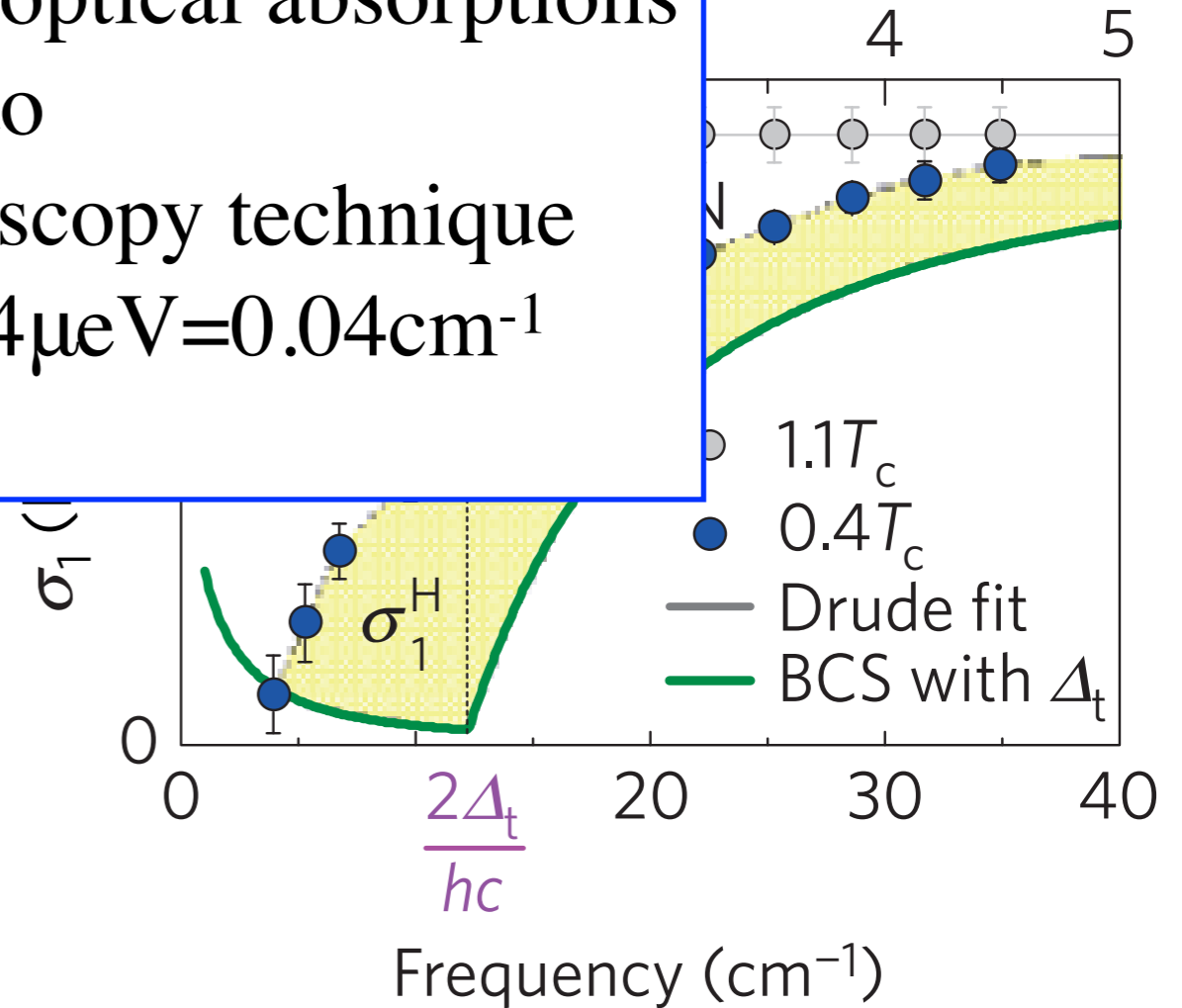
nature physics

The Higgs mode close to  $2\Delta$   
D. Sherman and al

Exc

present study (on grAl)  
various resolved sub-gap optical absorptions  
thanks to  
a NEW optical spectroscopy technique  
 $100\text{mK}$ ,  $\Delta E \sim 1\text{GHz} = 4\mu\text{eV} = 0.04\text{cm}^{-1}$

as:



PRB

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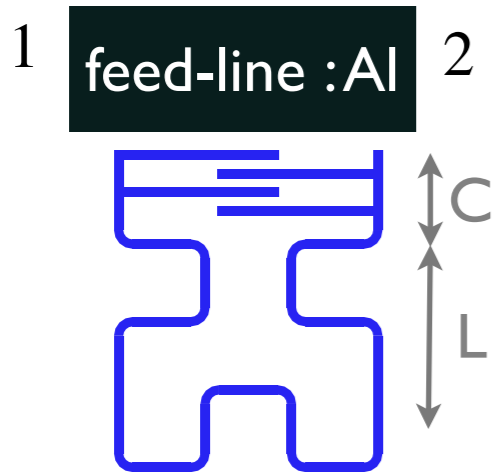
# Optical spectroscopy with superconducting resonators

KIDS  
 $h\nu > 2\Delta$

RLC resonator:  
 design and electrical measurement

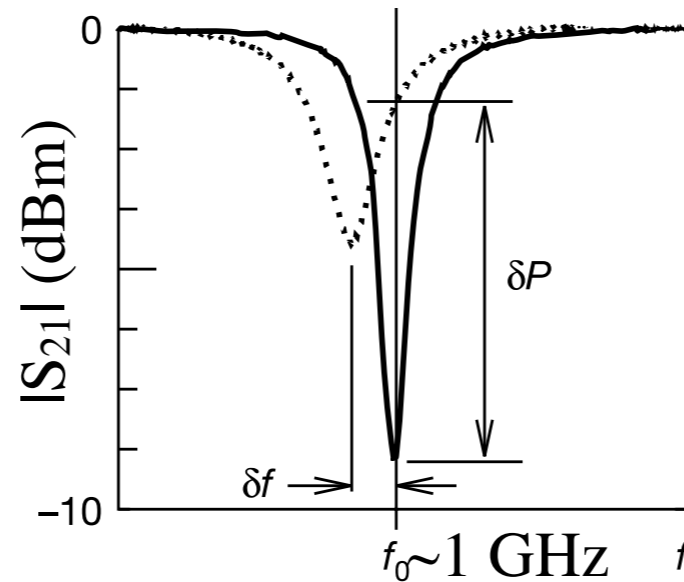
photon detection principle :  
 $h\nu > 2\Delta$

from Day et al, Nature 425, 817 (2003)

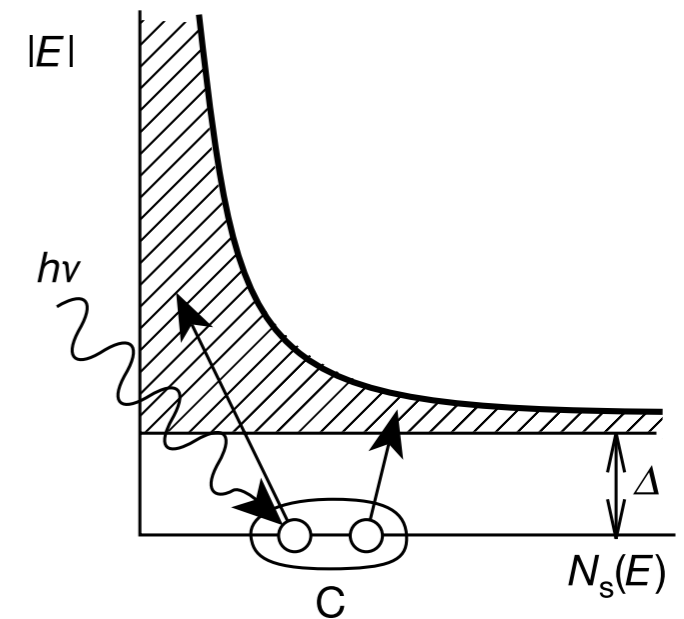


superconducting resonator

thin film ~tens of nm  
 substrate=Si, MgO, Al<sub>2</sub>O<sub>3</sub>,...



$$f_0 = (LC)^{-1/2}$$



**L ~ kinetic inductance of the superfluid**  
 $L \sim 1/n_s$

# Optical spectroscopy with superconducting resonators

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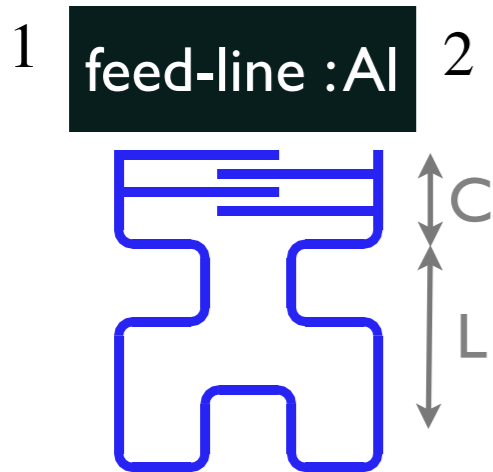
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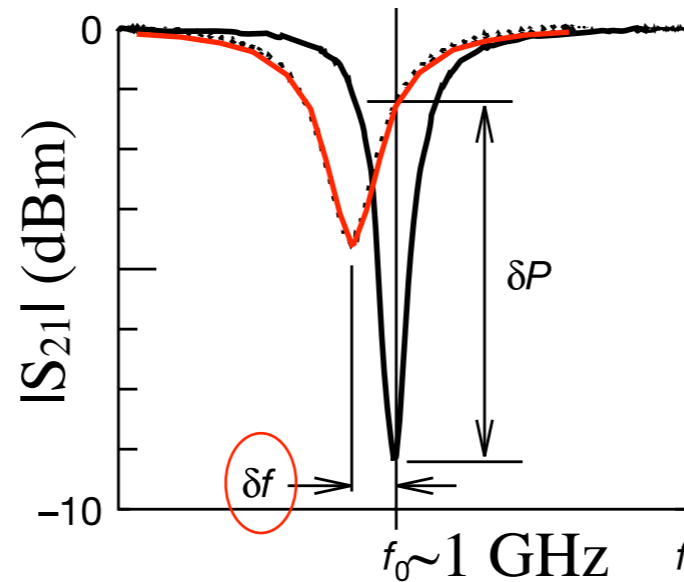
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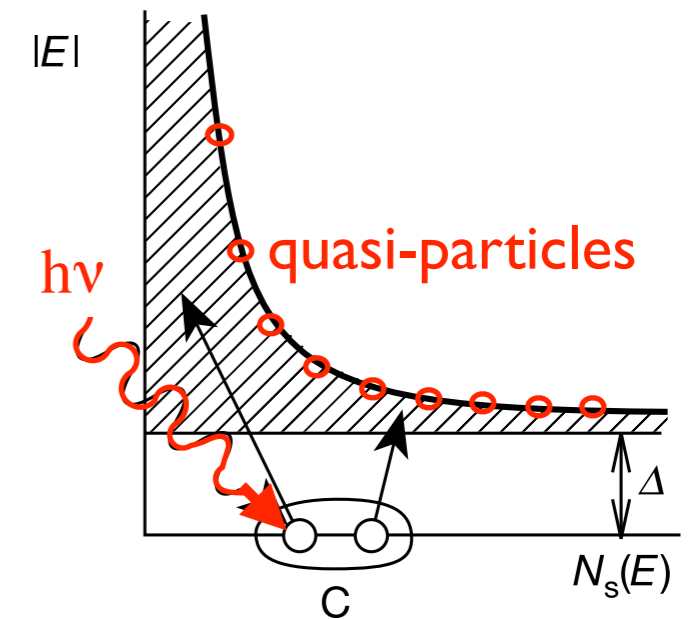
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frequency shift:  $\delta f$  due to  $n_s \downarrow$

Q-factor  $\downarrow$  due to dissipation  $\uparrow$

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# Optical spectroscopy with superconducting resonators

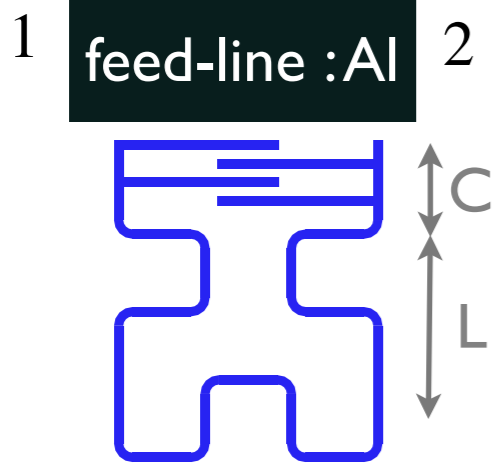
**KIDS**  
 $h\nu > 2\Delta$

RL Kinetic Inductance Detector : KID

on principle :

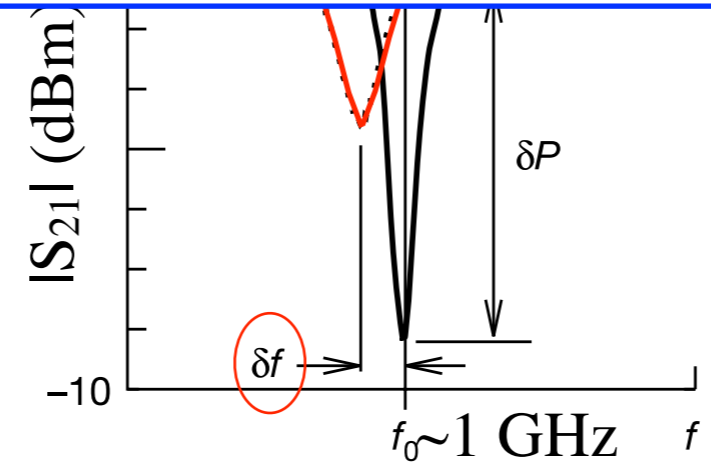
design and e

detection  $h\nu > 2\Delta$  through  $\delta f$

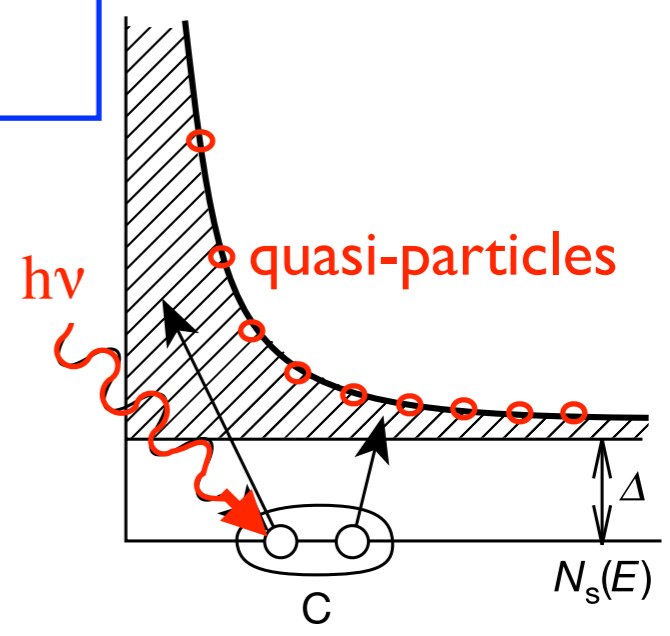


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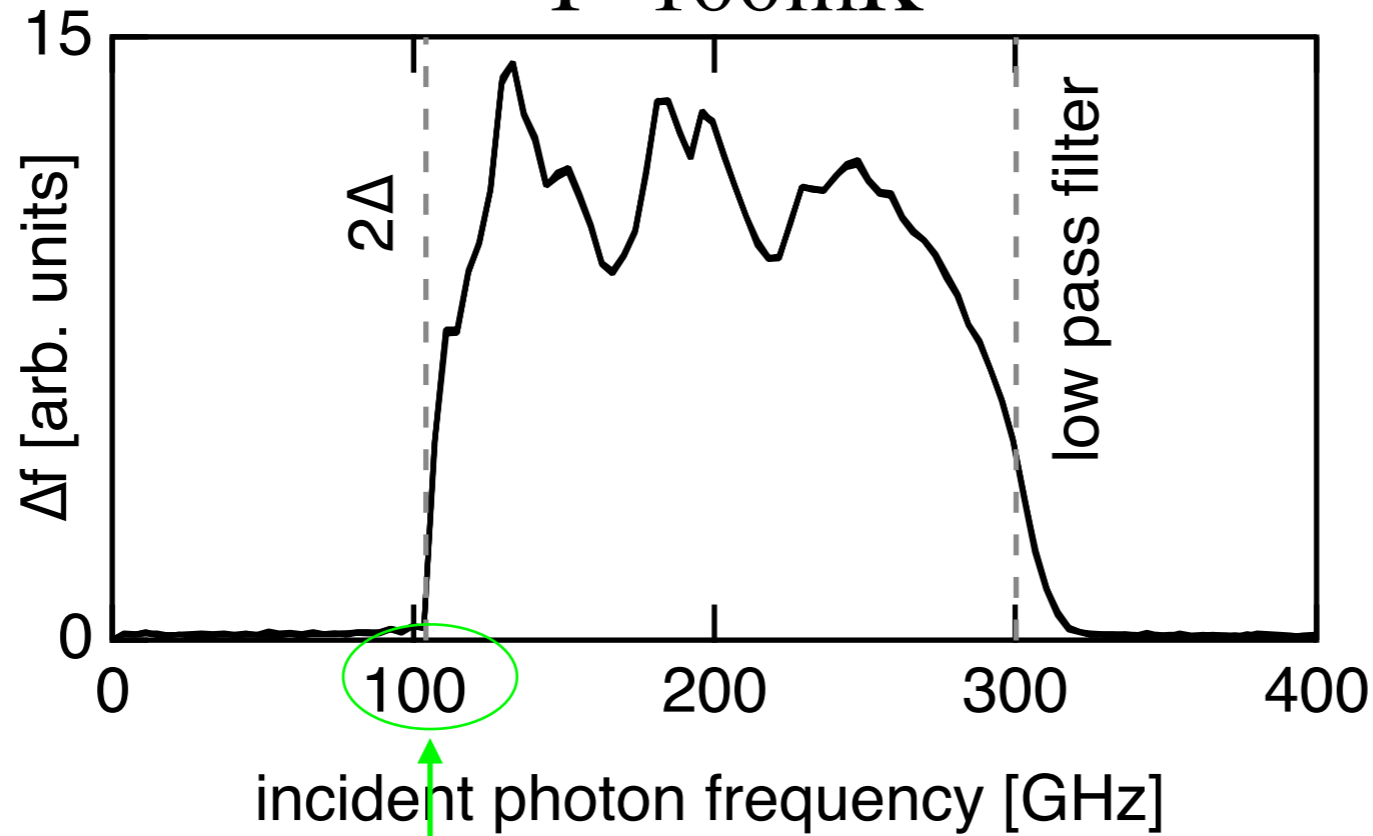


# Optical spectroscopy with superconducting resonators

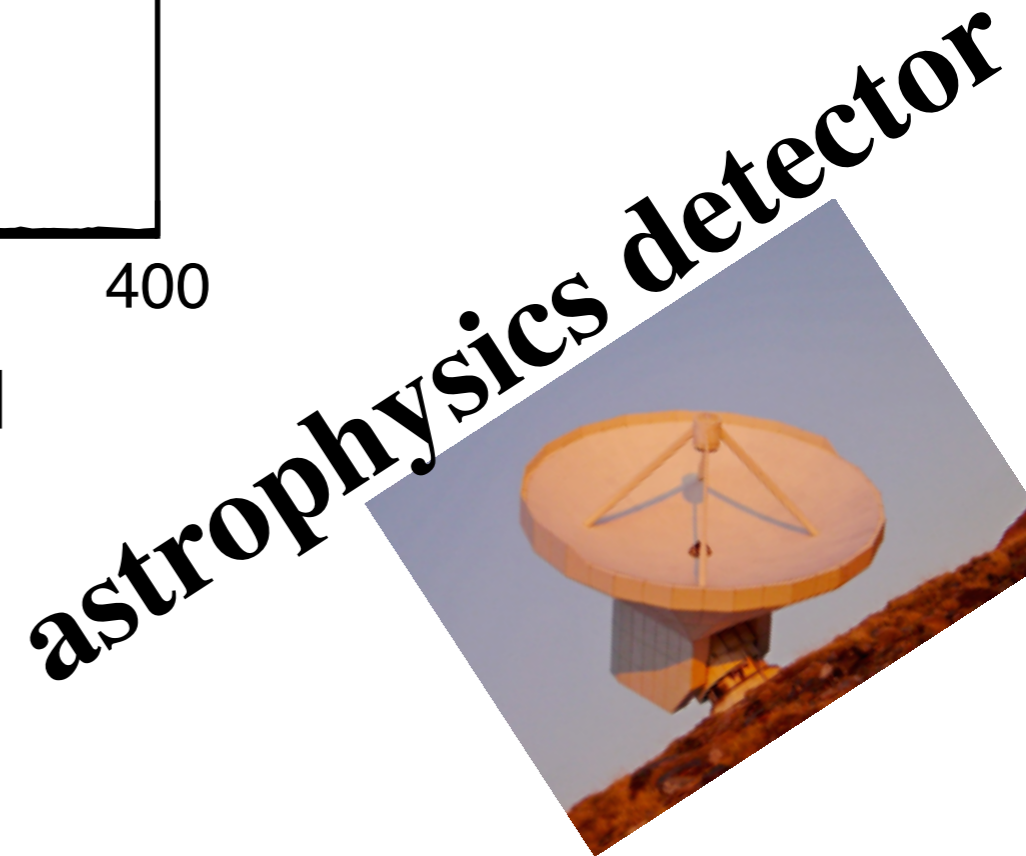
KIDS  
 $h\nu > 2\Delta$

pure Al 20nm-thick

T~100mK



For bulk Al:  
 $T_c = 1.2\text{K}$ ,  $2\Delta = 85\text{ GHz}$

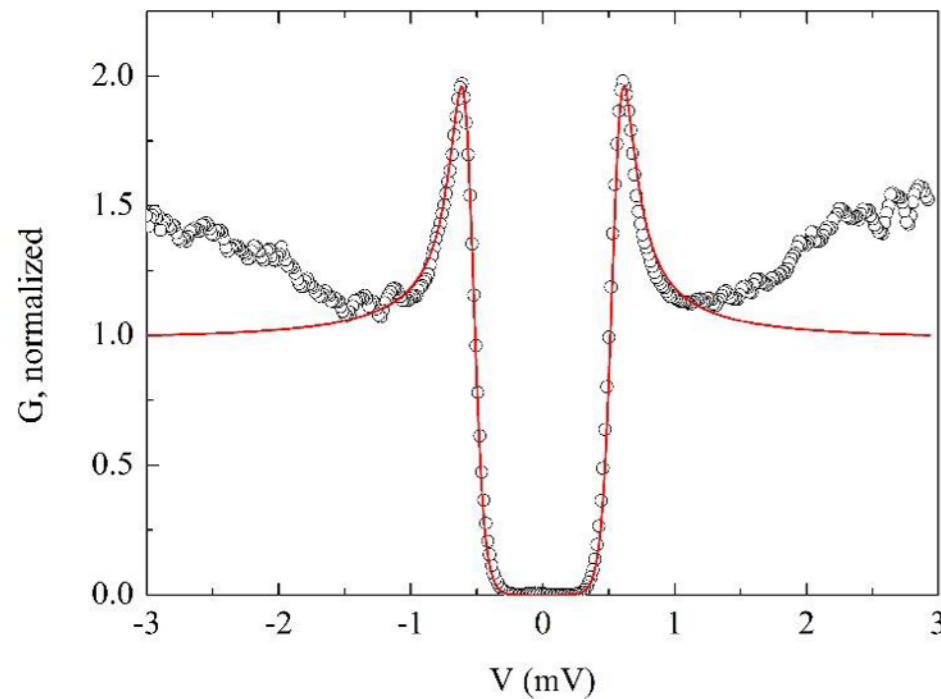


# Optical spectroscopy with superconducting resonators

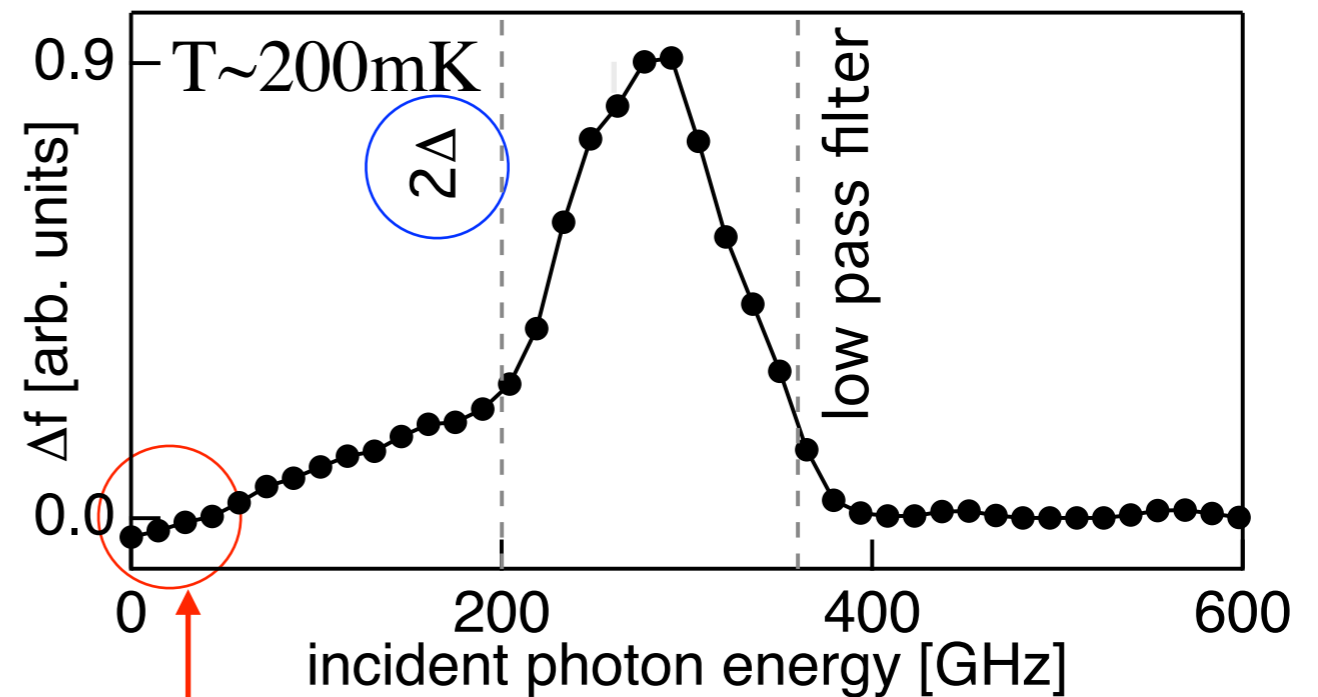
SKIDS  
 $h\nu < 2\Delta$

present a:InO<sub>x</sub>:  
T<sub>c</sub> ~ 2.8K, 2Δ ~ 260 GHz<sup>1</sup>

<sup>1</sup> Sacépé et al, PRB 91, 220508 (2015)



unpublished



detailed study

2Δ: STM and optical spectroscopy agreement

# Optical spectroscopy with superconducting resonators

SKIDS  
 $h\nu < 2\Delta$

Tuna

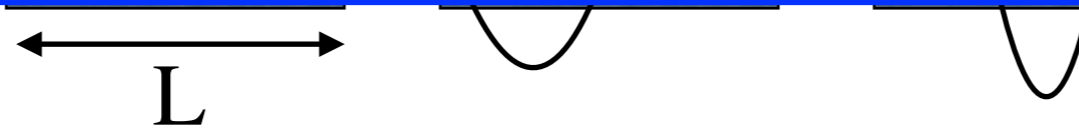
=

sonators

SKID : Sub-gap Kinetic Inductance Detector (17).

a:InOx

detection through  $\delta f$  for a specific  $h\nu < 2\Delta$



- $h\nu$ -selection = resonance mode (or any collective mode?)
- $h\nu$ -absorbed
  - > superfluid current density  $J$  increases
  - > superfluid density  $n_s$  decreases
  - > kinetic inductance  $L_k \sim 1/n_s$  increases
  - > resonance frequency shift

$$L(J) = L(0) [1 + J^2/J_*^2 + ..]^{1,2} \quad J_* = 2/3^{3/2} J_c$$

<sup>1</sup> see any textbook on superconductivity (de Gennes, Tinkham)

<sup>2</sup> L. Swenson et al, J. Appl. Physics 113, 104501 (2013)

**low  $J_c$  is *a priori* more adapted for sub-gap detection**

# Optical spectroscopy with superconducting resonators

SKIDS  
 $h\nu < 2\Delta$

Tunable sub-gap radiation detection with superconducting resonators

O. Dupré et al, Supercond. Sci. Technol. 30, 045007 (2017).

a:InOx



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- $h\nu$ -absorbed
  - > superfluid current density  $J$  increases
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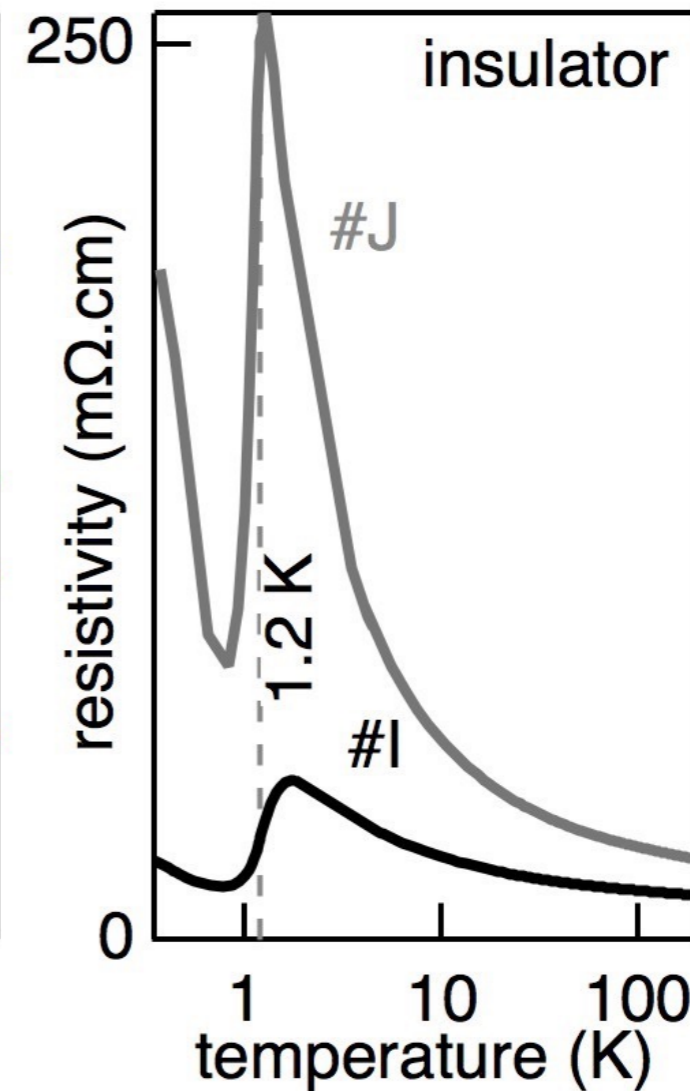
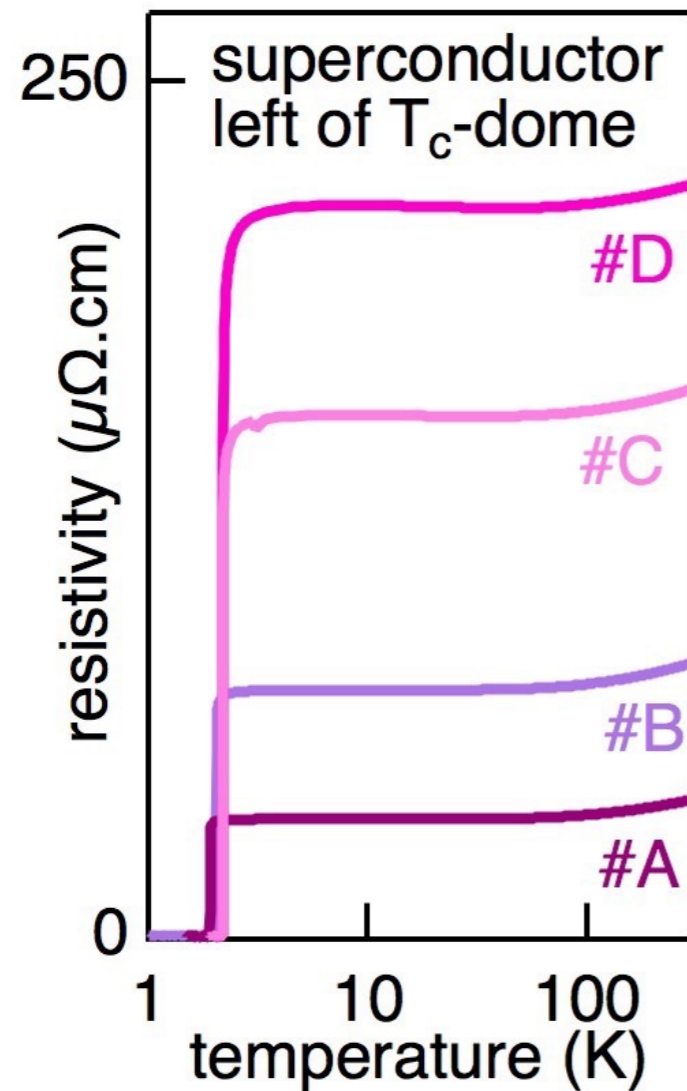
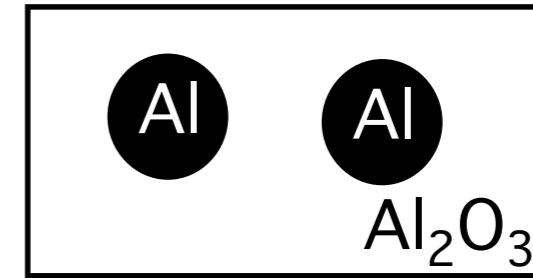
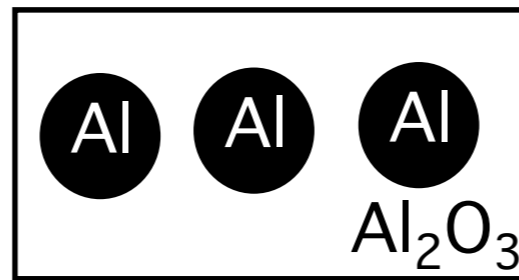
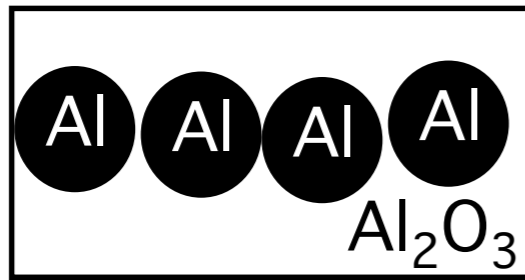
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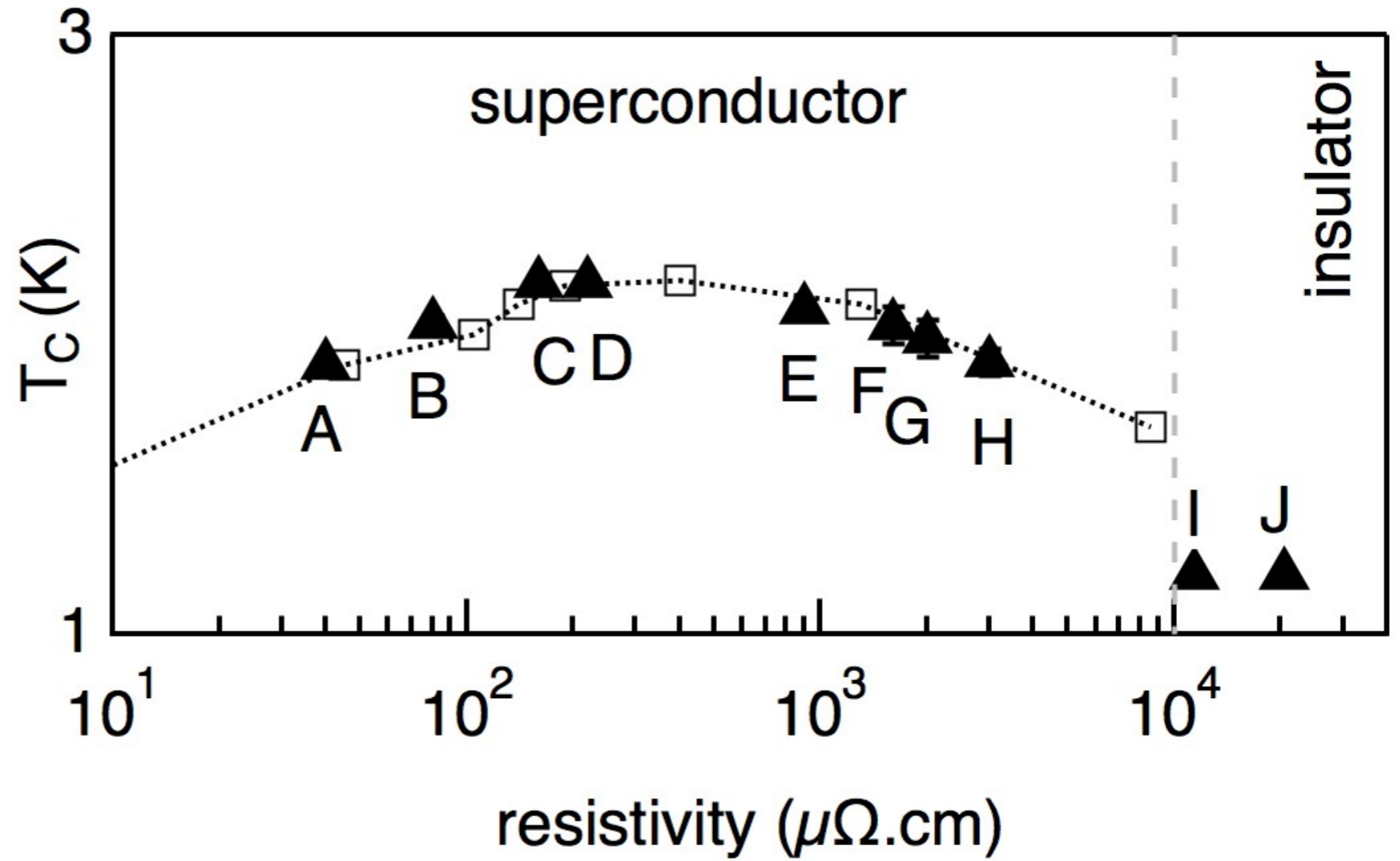
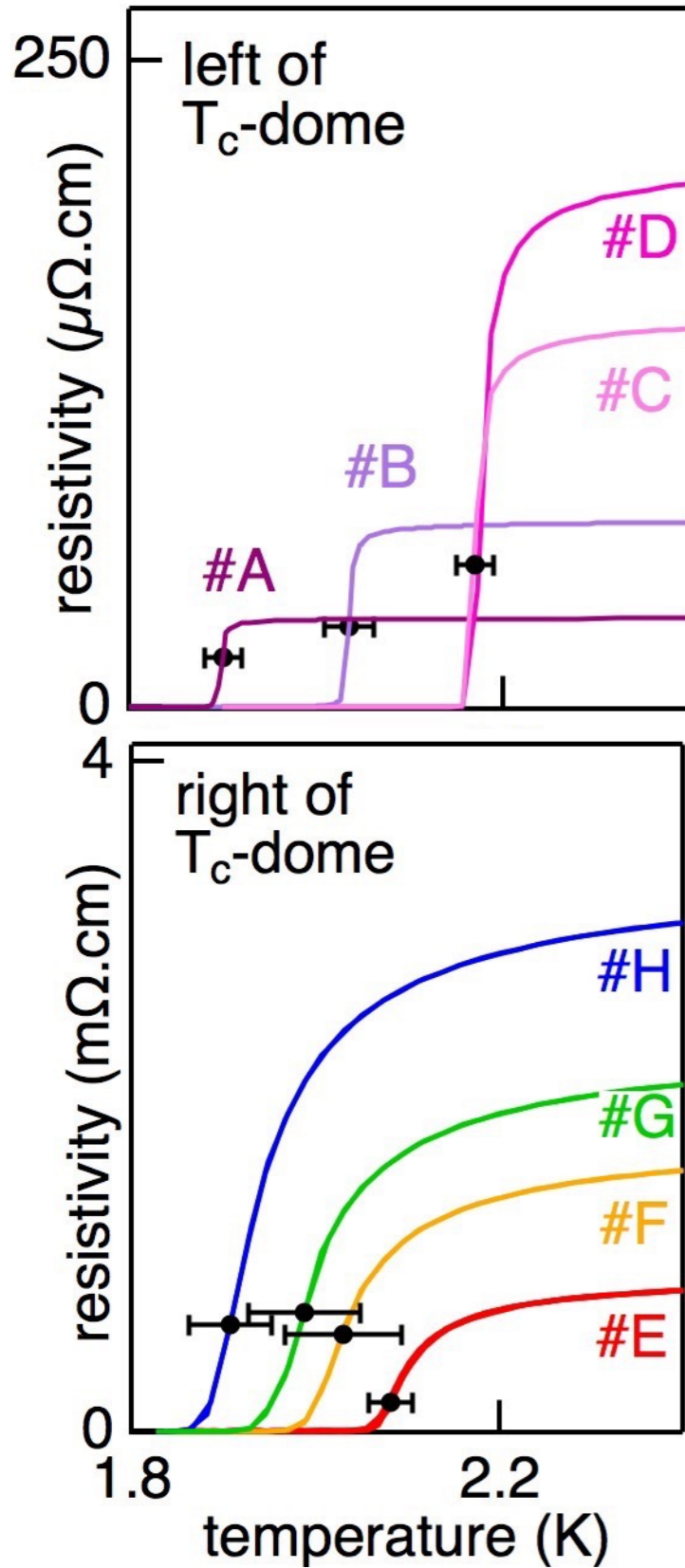
**low  $J_c$  is *a priori* more adapted for sub-gap detection**

# Granular Aluminium: resistivity



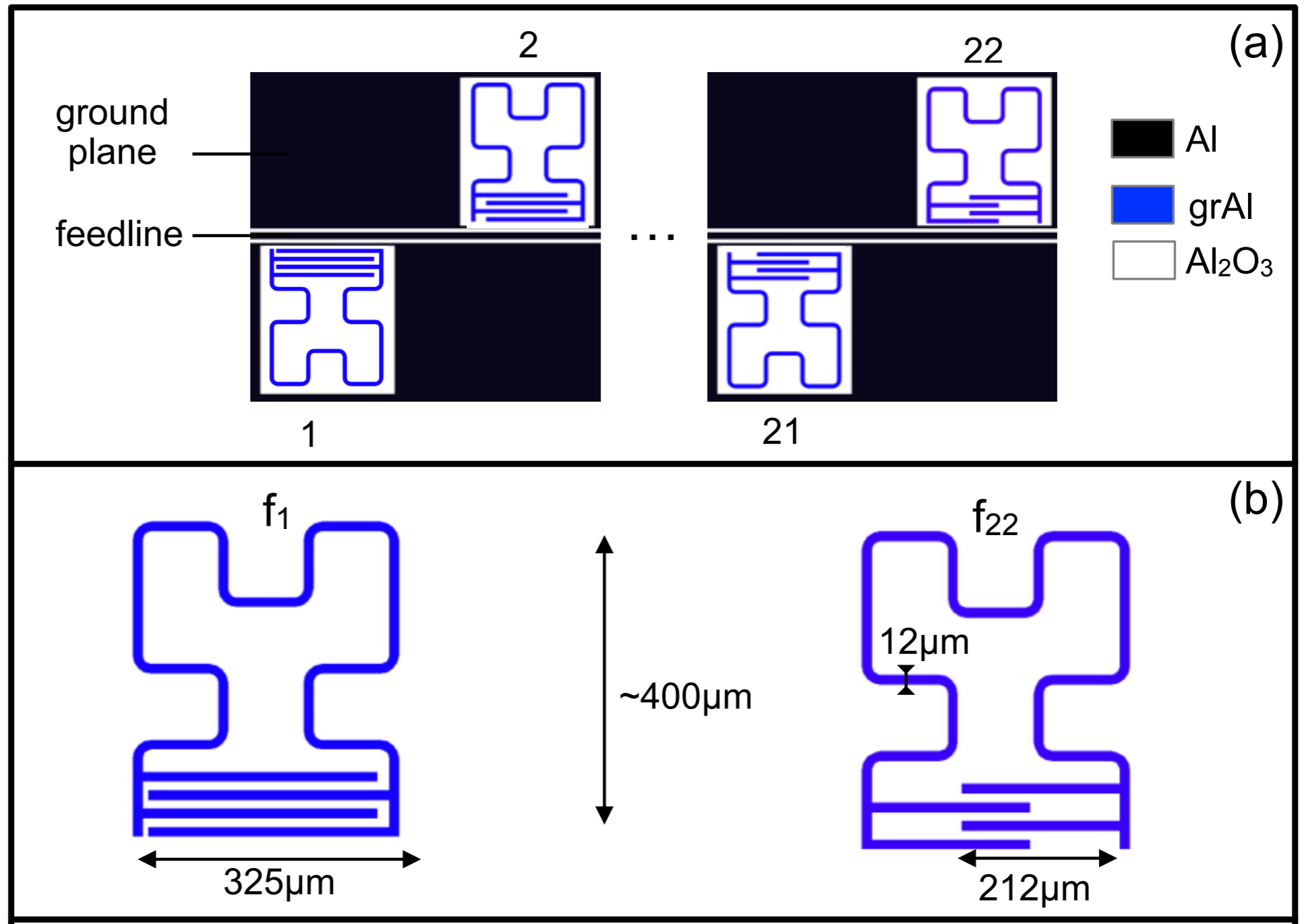


# Granular Aluminium: T<sub>c</sub> dome shape



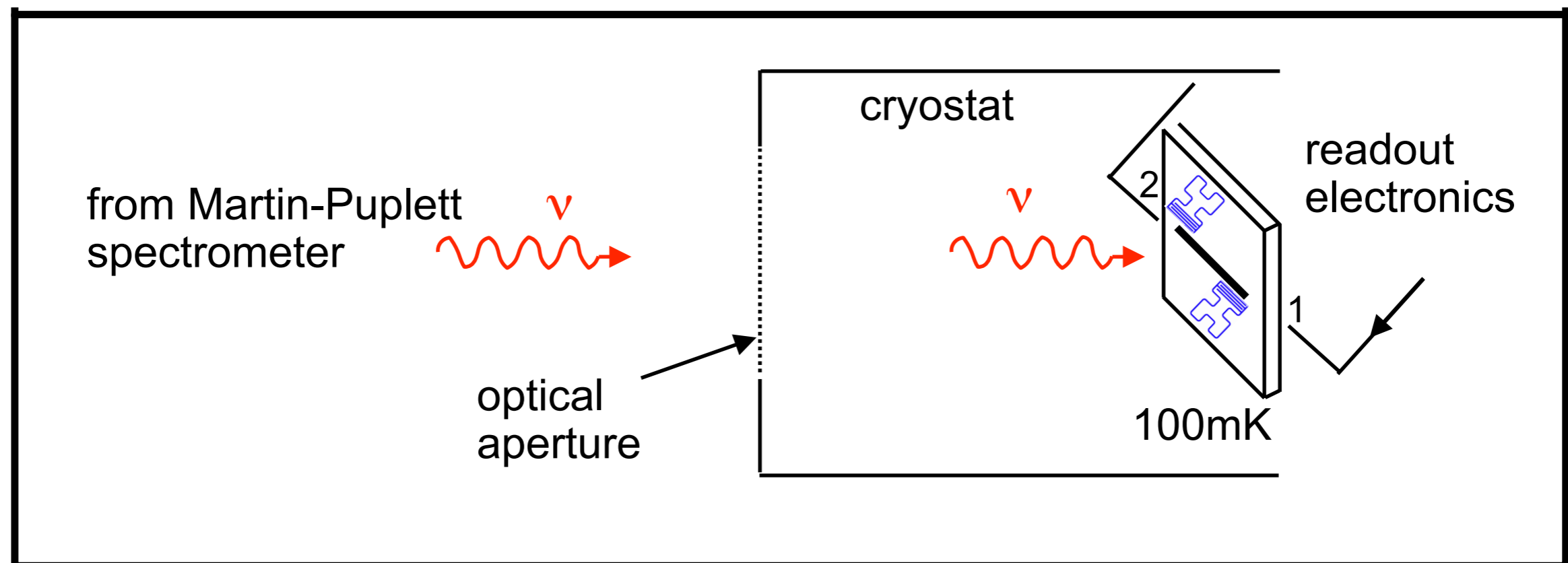
# Granular Aluminium: optical spectroscopy with superconducting resonators

Samples



# Granular Aluminium: optical spectroscopy with superconducting resonators

Set-up



source = 300K black body

Fourier-Transform spectrometry

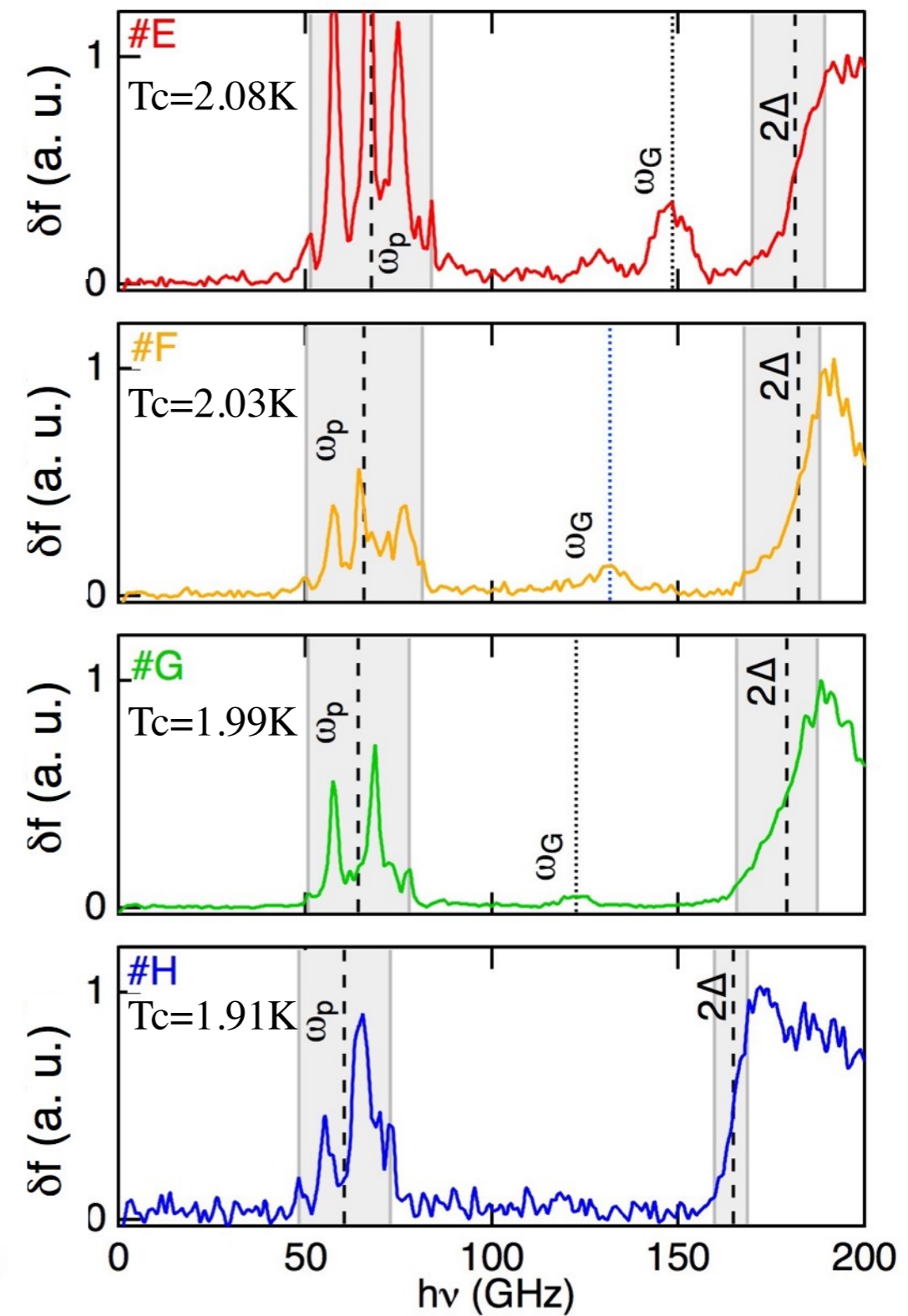
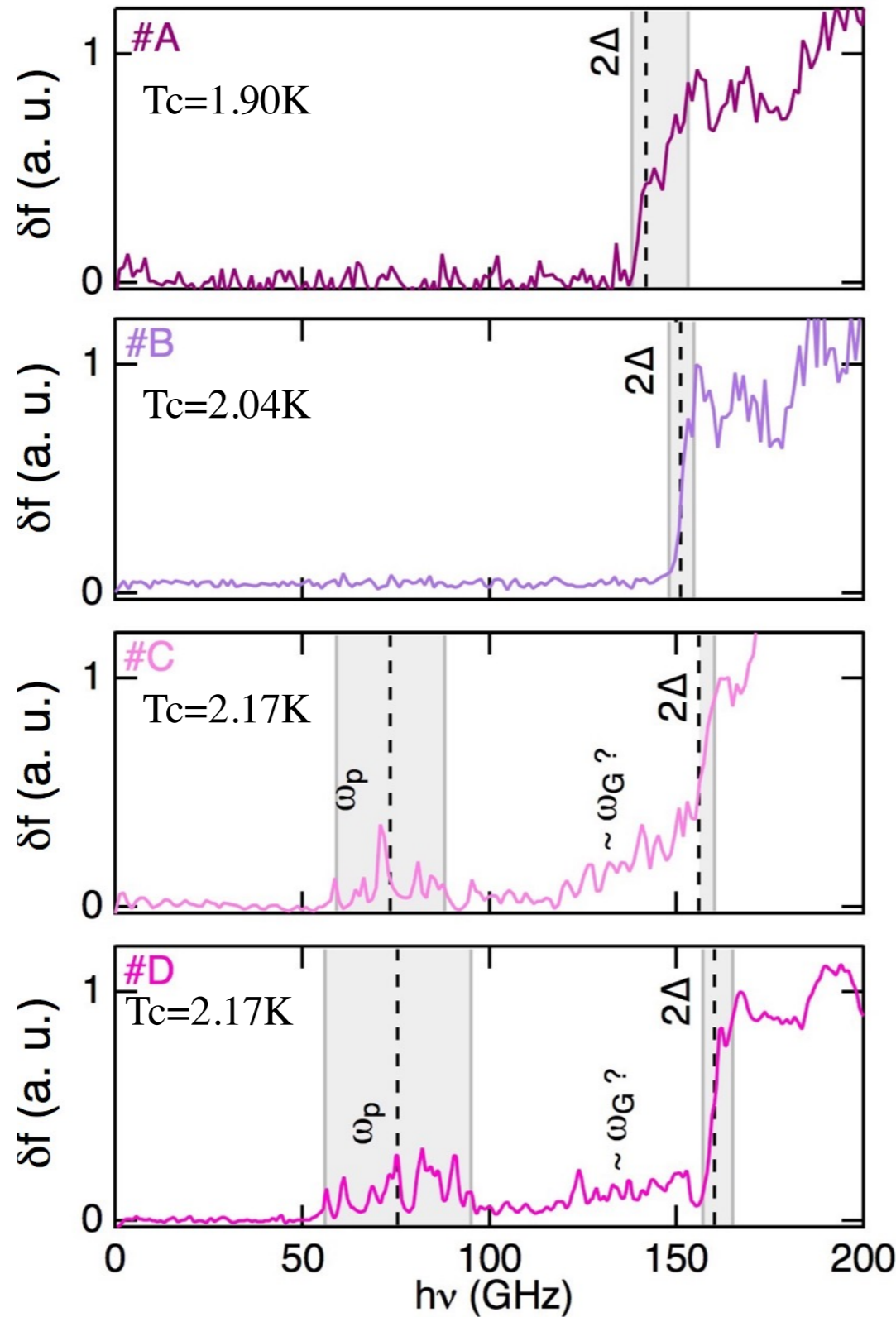


# Granular Aluminium: optical spectroscopy

left of Tc-dome

right of Tc-dome

$T_{\text{mes}} \sim 100 \text{ mK}$



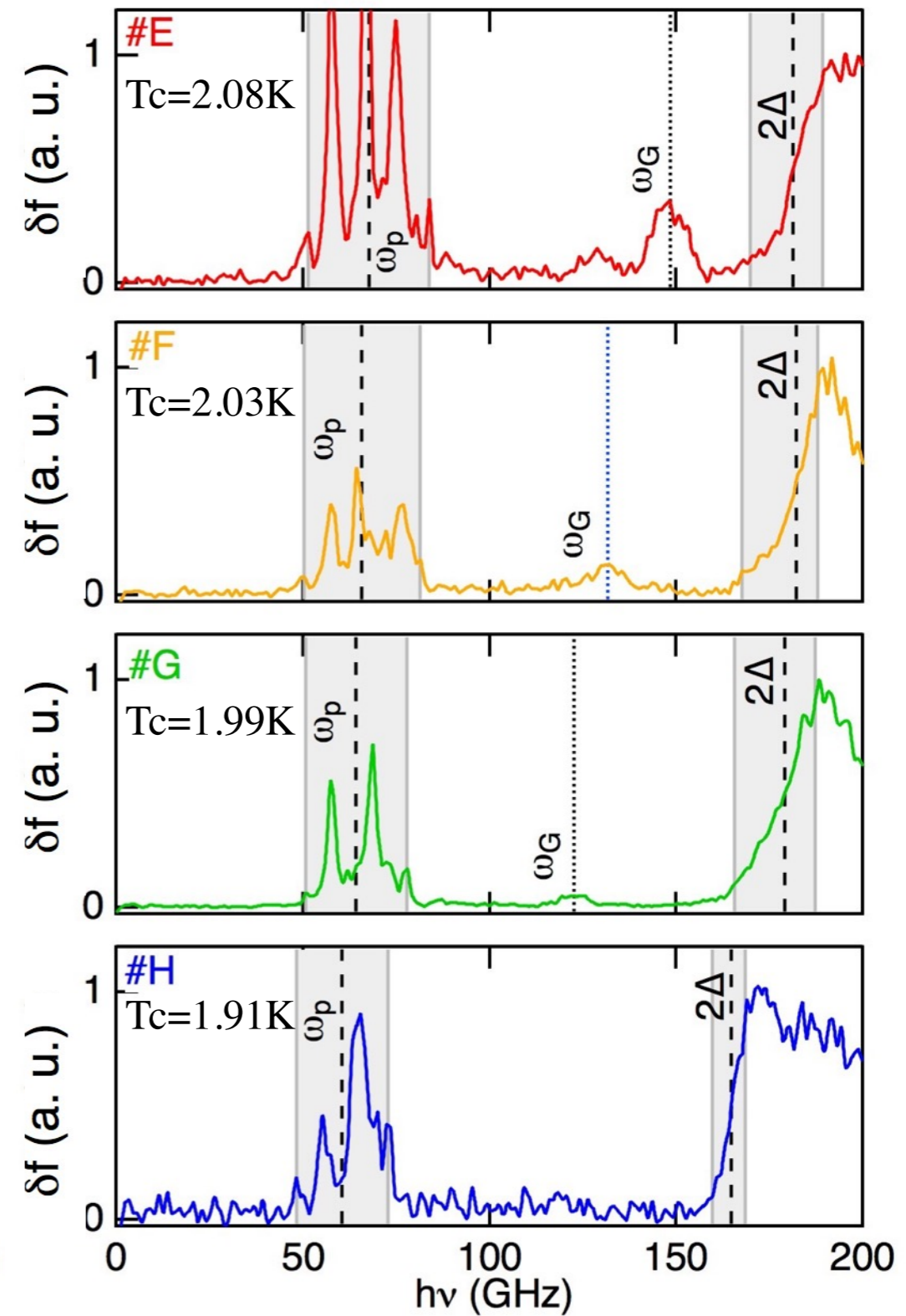
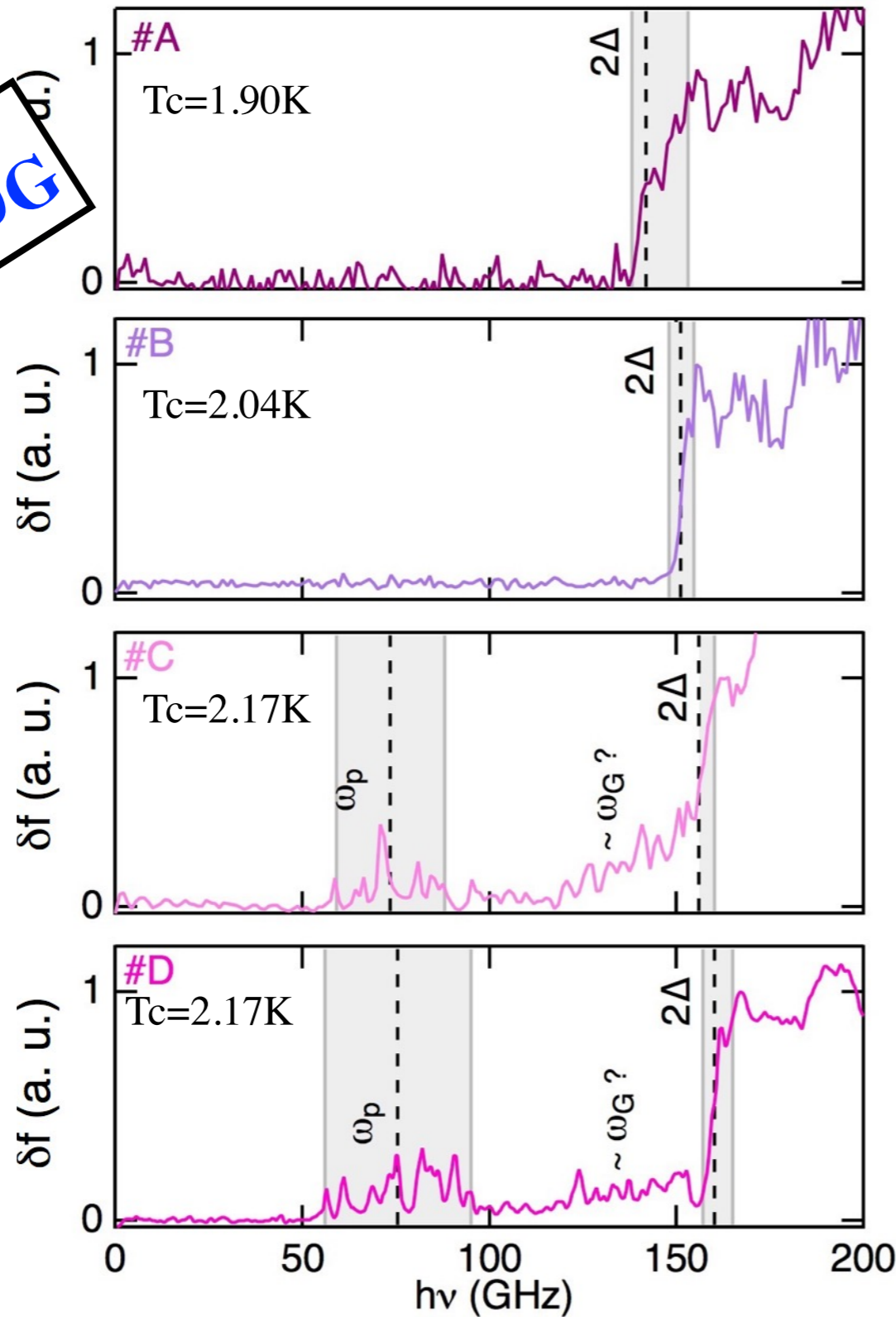
# Granular Aluminium: optical spectroscopy

left of Tc-dome

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$T_{\text{mes}} \sim 100 \text{ mK}$

$2\Delta, \omega_p, \omega_G$



# Granular Aluminium: phase stiffness $J$

= Josephson energy

$$J = \frac{\hbar}{4e^2} \frac{\pi \Delta}{R_{sq}} \longrightarrow J_{\Delta} \text{ from measurements}$$

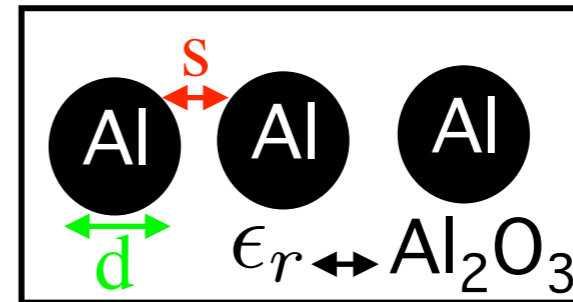
||

$$J = \frac{\hbar^2}{4e^2 L_s} \longrightarrow J_{L_s} \text{ from kinetic inductance } L_s$$

$L_s$  obtained by RF-simulation  
adjusting the actual  
resonance frequencies  $f=(LC)^{-1/2}$

# Granular Aluminium: Coulomb $E_c$

$$E_c = \frac{e^2}{4\pi\epsilon_0\epsilon_r d} \frac{s}{s + d/2}$$



$$d = 3\text{nm} - 6\text{nm}$$

$$s = 0.5\text{nm}$$

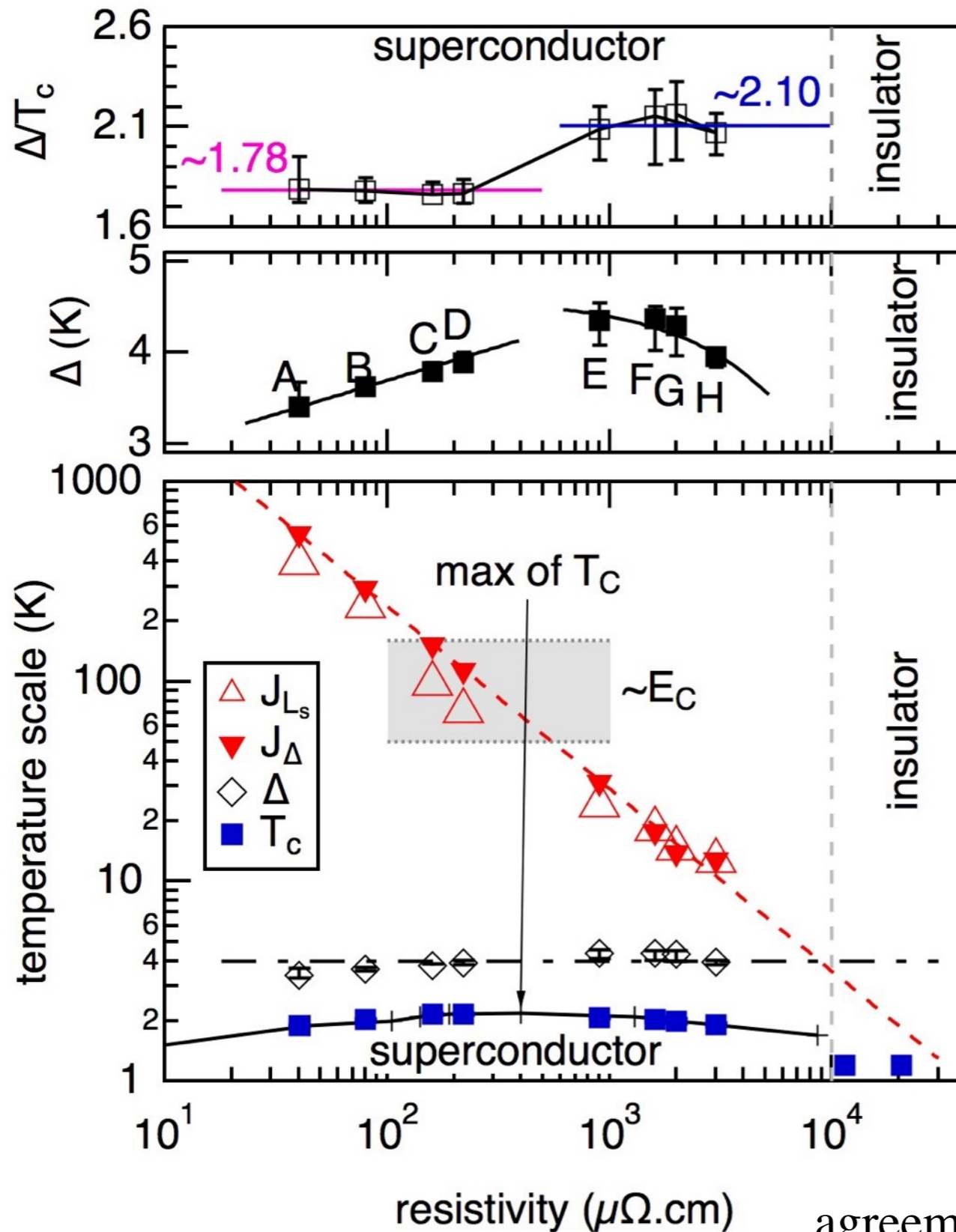
$$\epsilon_r = 8.5$$



$$E_c \sim 100 \pm 50 \text{ K}$$



# Granular Aluminium: phase diagram



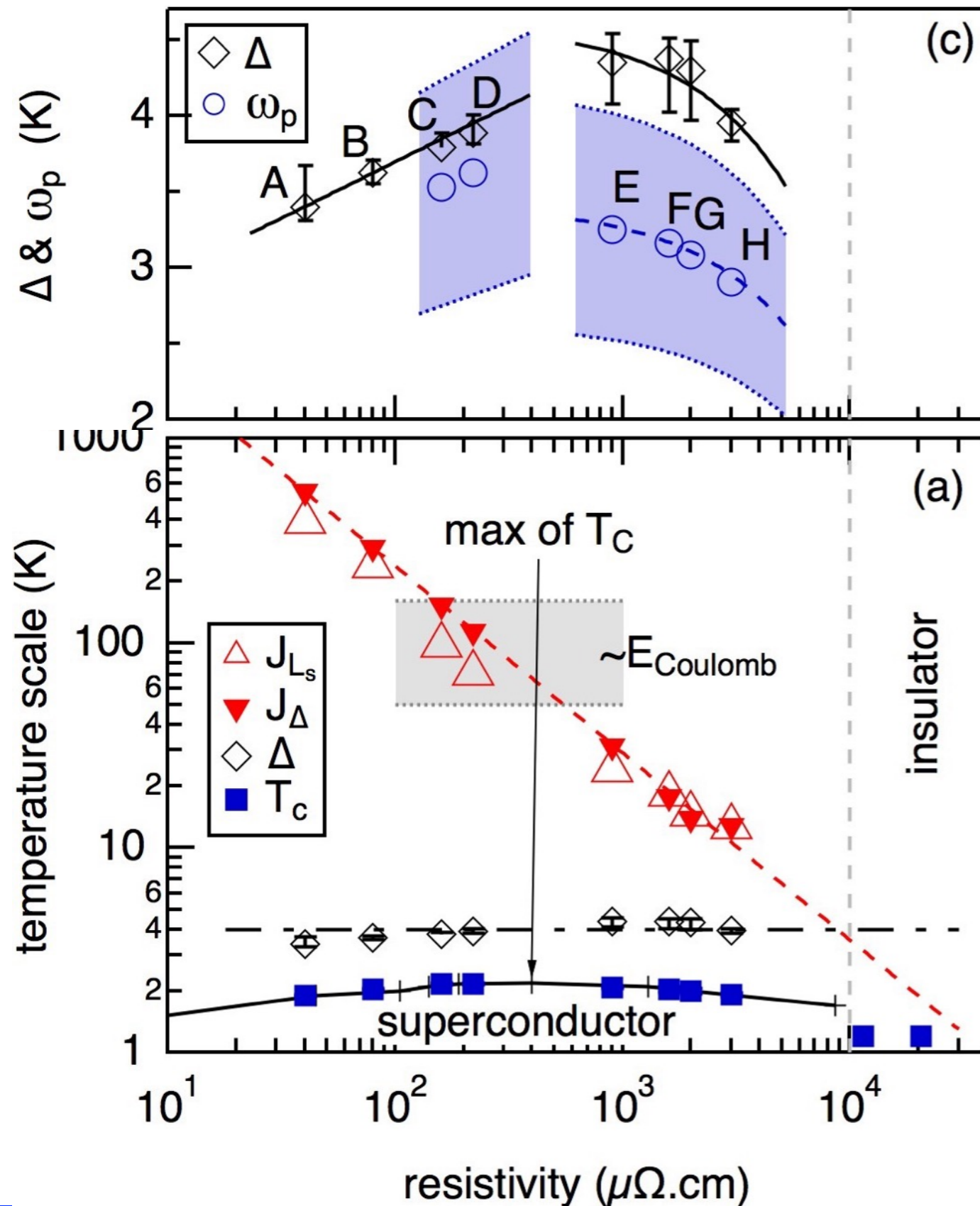
## interplay of $J$ , $E_c$ and $\Delta$

- $J > E_c$ :  
“metal”  
 $\Delta/T_c \sim 1.78$
- $\Delta < J < E_c$ :  
“non-metal”  
 $\Delta/T_c \sim 2.10$   
sub-gap absorptions
- $J < \Delta$ :  
insulator

agreement with Pracht and al, PRB 93, 100503(R) 2016.

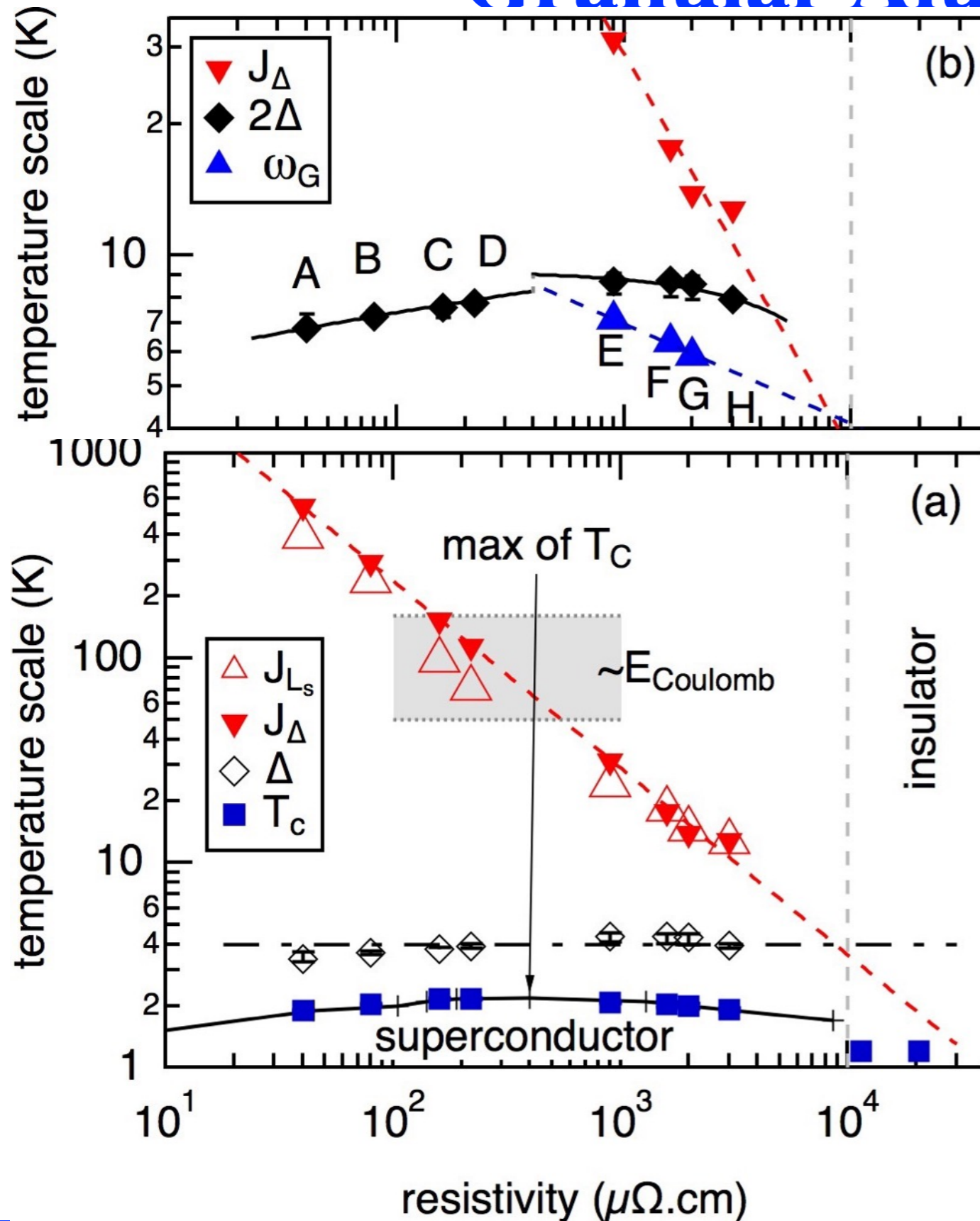
# Granular Aluminium: $\omega_p$

## Scaling of $\omega_p$ with $\Delta$



# Granular Aluminium: $\omega_G$

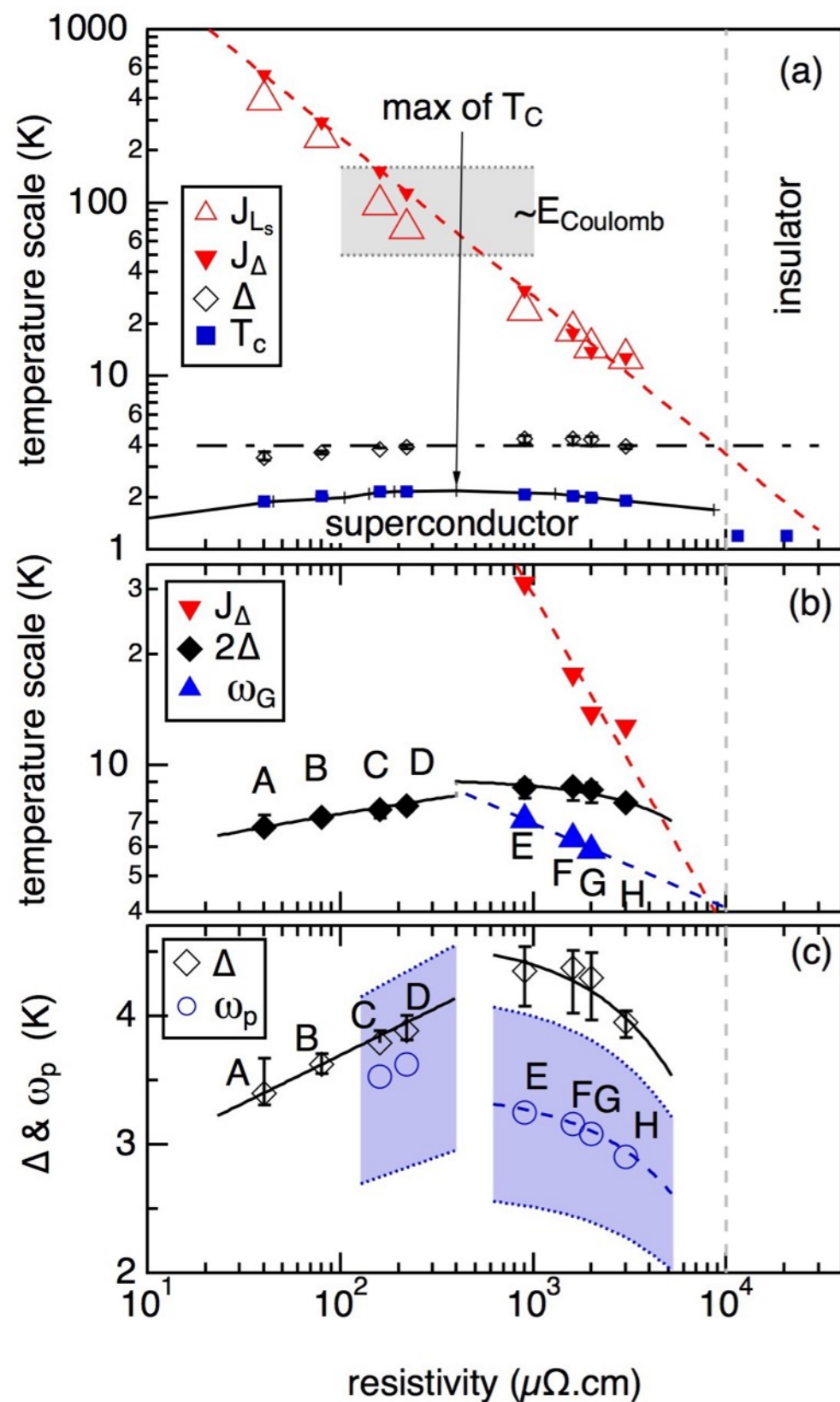
Scaling of  $\omega_G$  with  $J$   
(?)





# Granular Aluminium

discussion



- sub-gap optical absorption in agreement with literature but now resolved features

- onset when  $J \lesssim E_c$   
suggest phase fluctuations

- literature explains 1 mode  
observation of 2 (or more?) modes

- **N. Maleeva and al, Nat. Com 9, 3889 (2018)**  
 $\omega_p$  =saturation of 2D plasmon dispersion  
quantitative agreement but for multipеaks

- $\omega_G$  ? ...



# Conclusion

- Sub-gap modes in (various) superconductors
- Origin(s) under debate
- Of interests for 3 communities:
  - astrophysics instrumentation (photon detection)
  - quantum engineering (high- $L_K$  vs dissipation?)
  - fundamental studies

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**THANK YOU**